

# Optimal forest rotation with increasing carbon pricing

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# Forests and carbon pricing

- Forest in the carbon cycle:  
growth → sink,                      combustion or decay → emission
- Carbon flows could be priced to achieve economic efficiency

Past research on the impact of carbon pricing on forestry:

- Forest-owner's perspective:
  - van Kooten et al., 1995
  - Hoen and Solberg, 1997
  - Pohjola and Valsta, 2007
- As a part of the macroeconomy:
  - Tahvonen, 1995
  - Sohngen and Mendelsohn, 2003
  - Lintunen and Uusivuori, 2014

Constant carbon price  $P_c$

# Economically efficient mitigation

- Numerical mitigation scenarios:  
increasing carbon price, often exponentially
- Ekholm, 2014: price evolution for meeting 2°C cost-efficiently

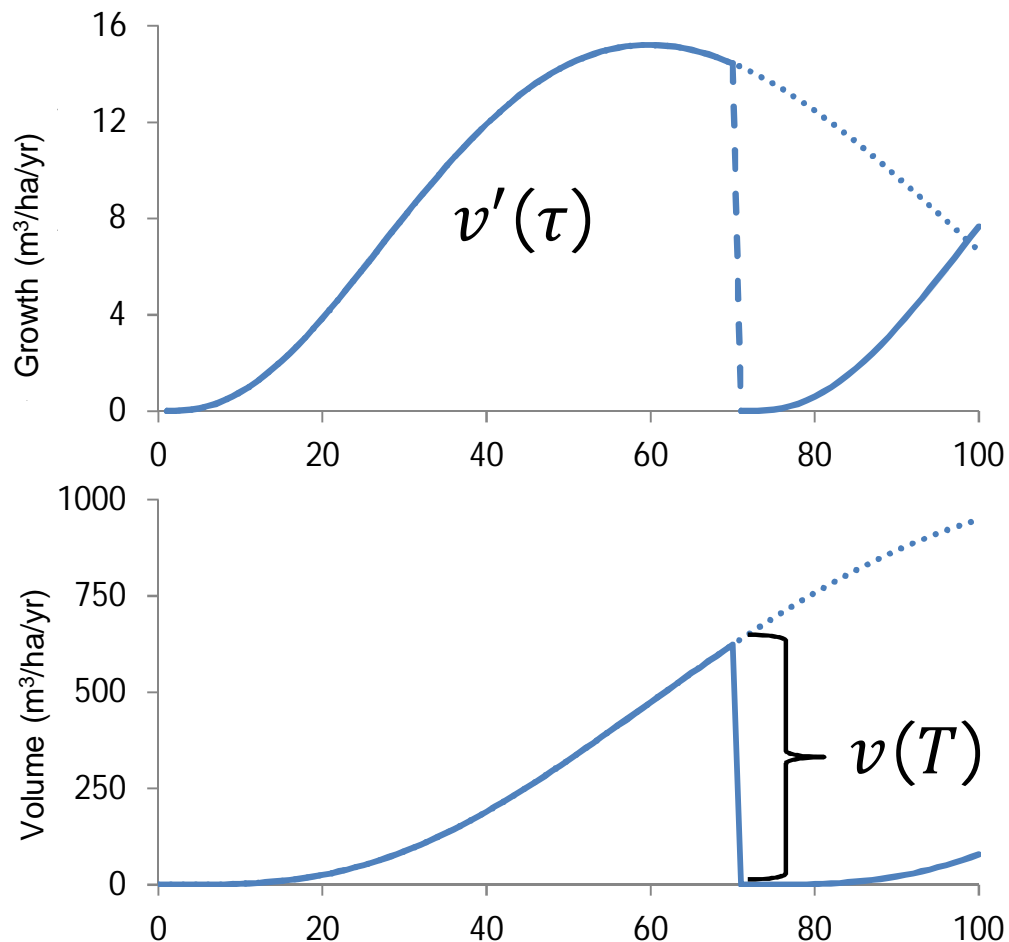
$$\begin{array}{c}
 \text{Current marginal cost} \quad \text{Future marginal cost} \quad \text{Impact of emissions} \\
 \text{to the 2°C target} \\
 \hline
 c'_t(r_t) = \beta E_t \left[ c'_{t+1,s}(r_{t+1,s}) \frac{\sum_{\tau=t+1}^{\infty} (I_s(t, \tau) \beta^{\tau-t-1} \lambda_{\tau,s})}{\sum_{\tau=t+2}^{\infty} (I_s(t+1, \tau) \beta^{\tau-t-1} \lambda_{\tau,s})} \right] \\
 \hline
 \text{Discount factor}
 \end{array}$$

(Climatic Change 127, pp. 153-167, [dx.doi.org/10.1007/s10584-014-1243-8](https://doi.org/10.1007/s10584-014-1243-8))

# The forest-owner's problem

- Maximize the revenues by choosing the timing of fellings
  - When to cut: the optimal forest rotation length  $T$ ?
- Things to consider:
  - Forest growth rate – the forest growth curve  $v(t)$  ( $\text{m}^3/\text{ha}$ )
  - Price of timber  $P_f$  ( $\$/\text{m}^3$ )
  - Price of carbon  $P_c$  ( $\$/\text{tC}$ ) and its annual growth rate  $\rho$
  - Discount rate  $r$
  - Regeneration costs  $C$  ( $\$/\text{ha}$ )
- But: carbon price changes over time
  - the optimal rotation lengths  $T_1, T_2, \dots$  differ

# Optimal rotation with increasing carbon pricing



Income from forest growth:

$$\int_0^T \alpha P_c e^{\tau(\rho-r)} v'(\tau) d\tau$$

Carbon content per volume

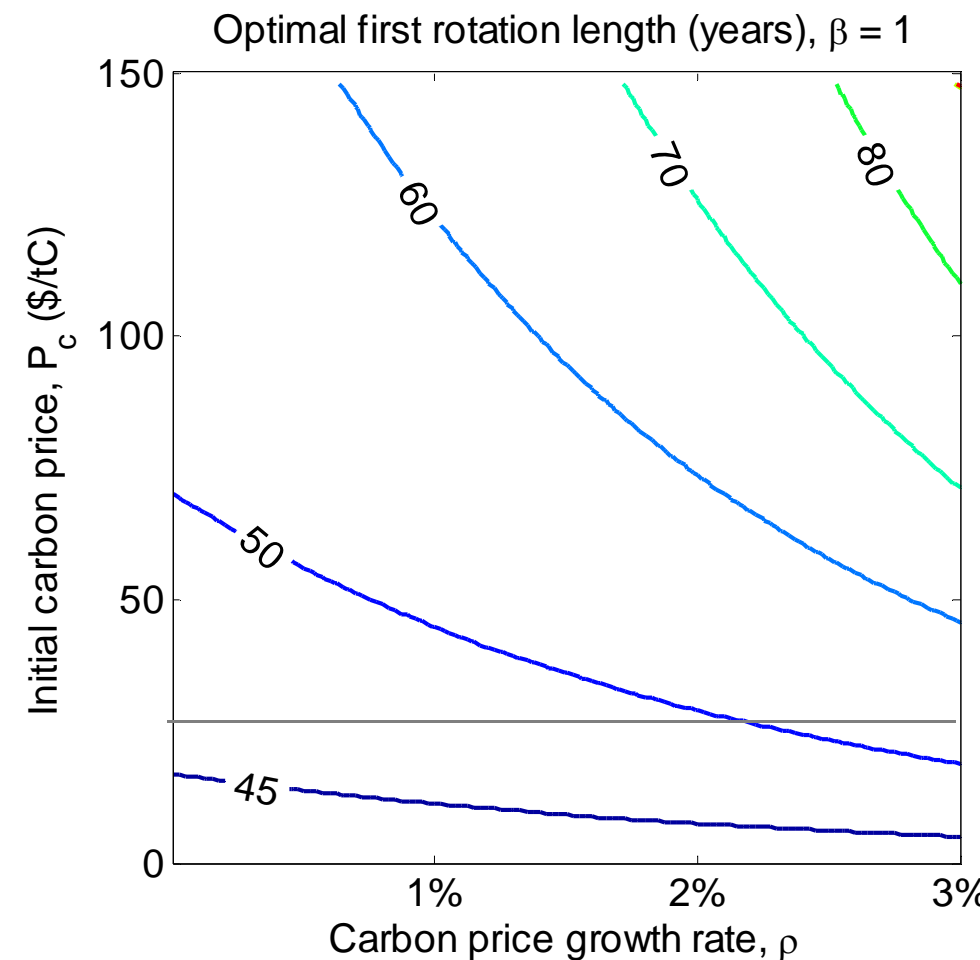
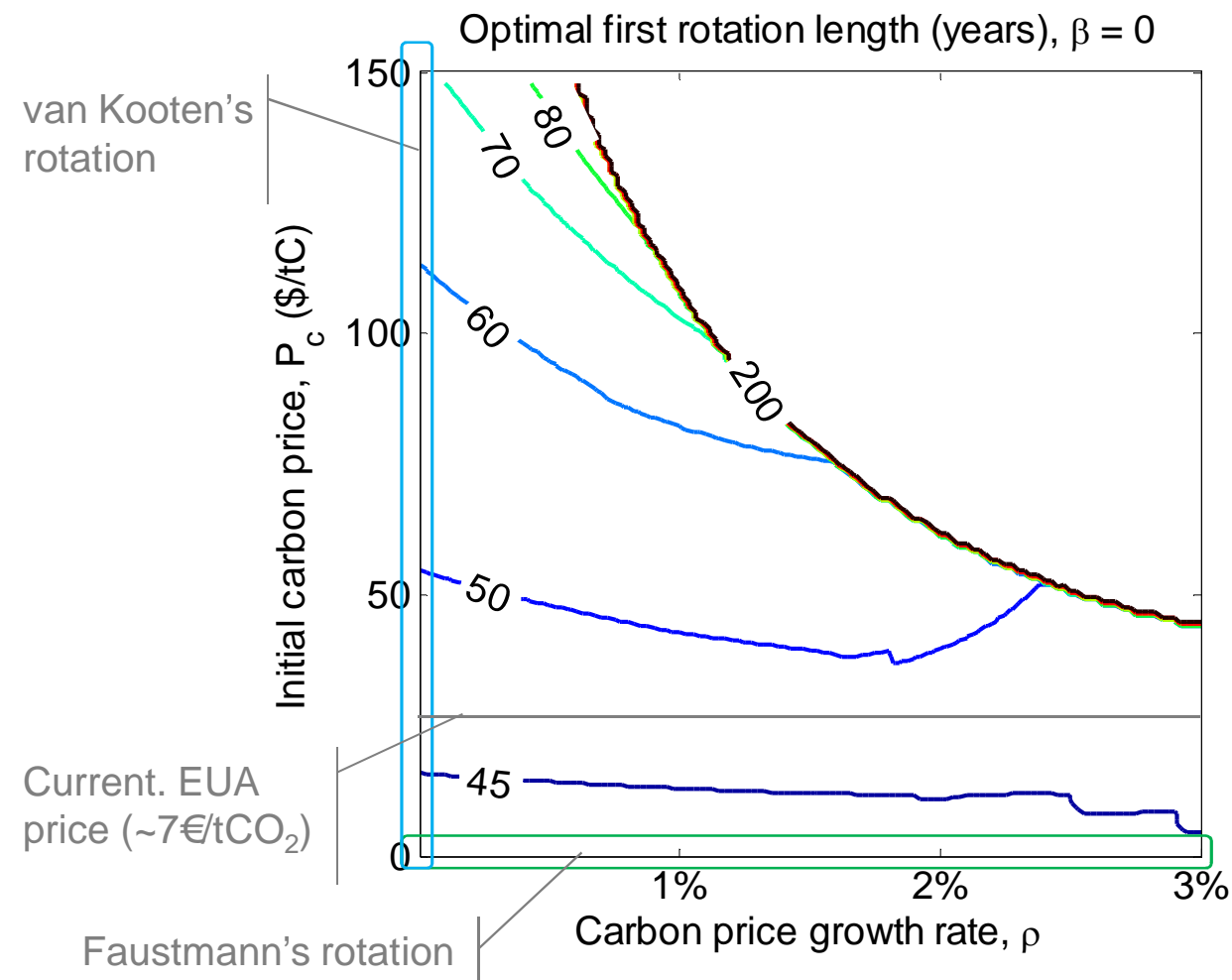
Net income from fellings:

$$e^{-rT} [(P_f - \alpha(1 - \beta)e^{\rho T} P_c) v(T) - C]$$

Share of carbon that is stored permanently

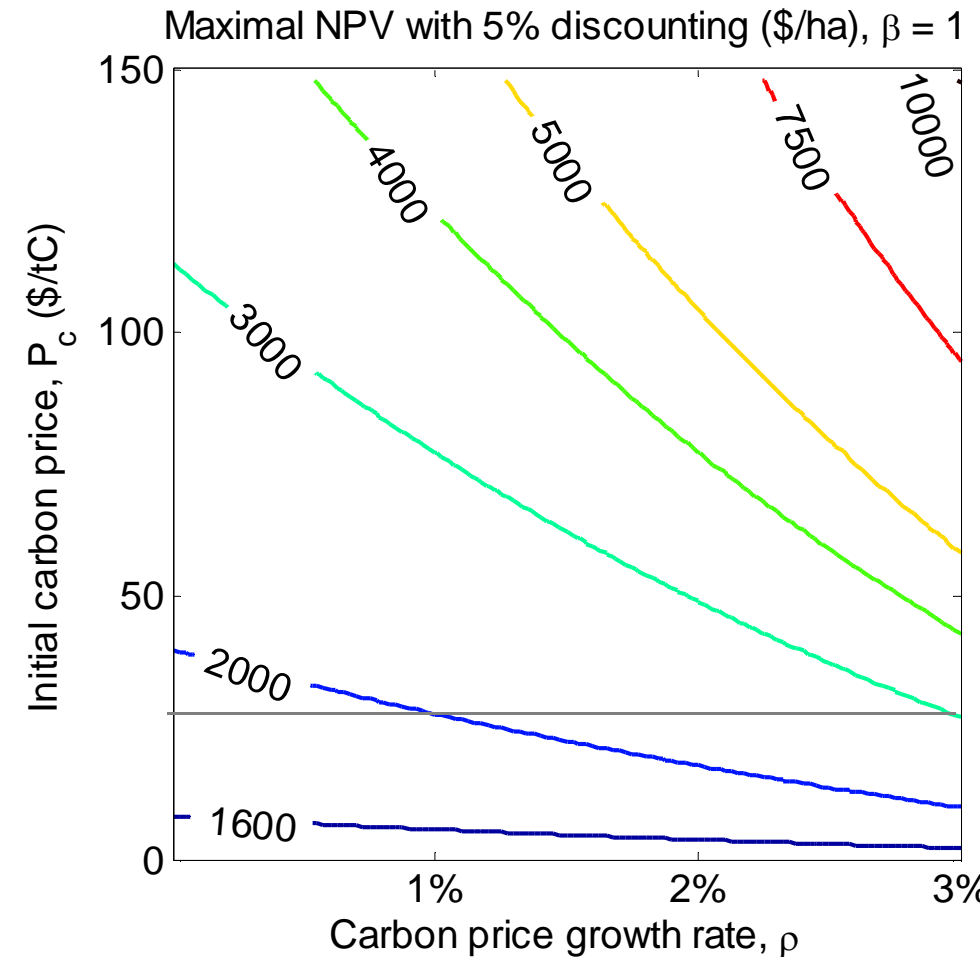
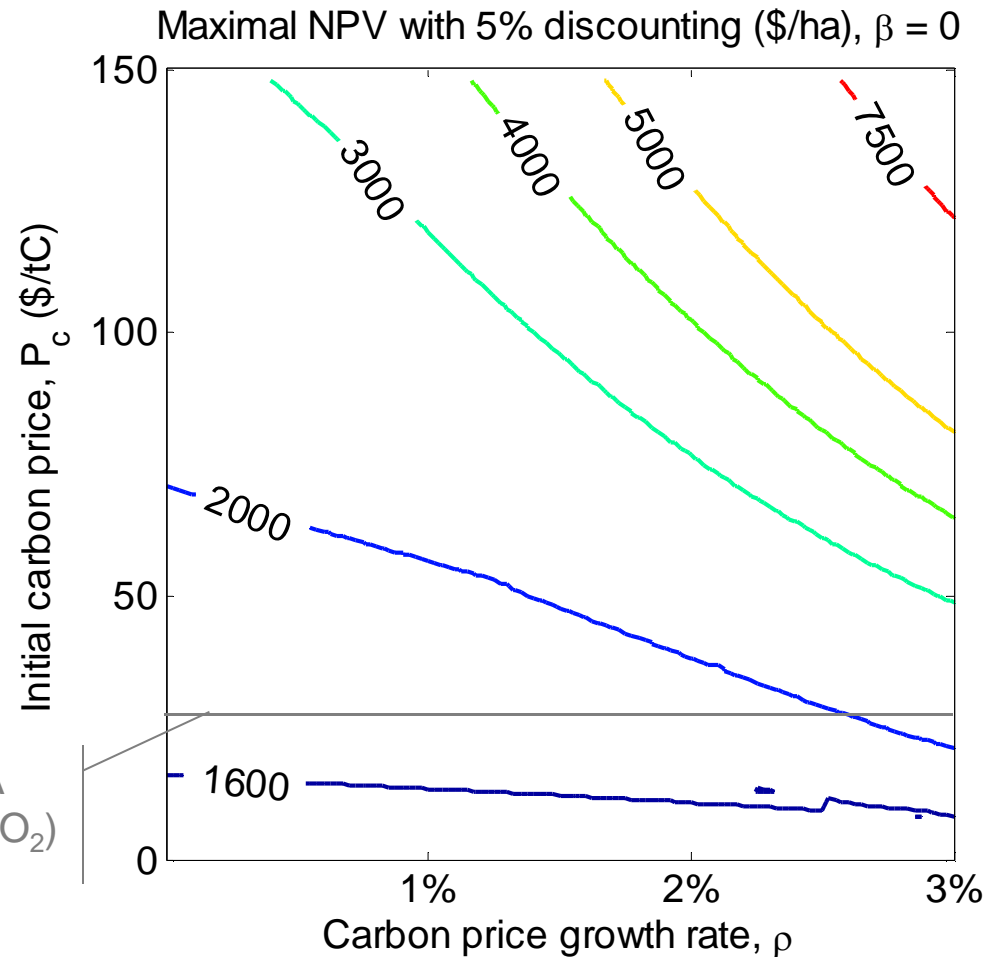
# Optimal length for the first rotation

Discount rate: 5%, timber price = 50 \$/m<sup>3</sup>, growth curve: van Kooten et al. (1995)



# Bare land value (\$/ha)

Discount rate: 5%, timber price = 50 \$/m<sup>3</sup>, growth curve: van Kooten et al. (1995)



## Final remarks

- $P_c$  and  $\rho$  both increase rotation lengths and land value
- If carbon is released to the atmosphere ( $\beta = 0$ ), the optimal rotation might be lengthened to “infinity”
  
- A number of important aspects not considered here:
  - Increasing price for timber
  - Forest management, e.g. thinnings
  - Risks of forest fires etc. damages
  - Uncertainty, particularly for carbon pricing





**Thank you!**

**Comments, questions:  
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